

LANL PLASMA JET WORKSHOP, JANUARY 24-25 2008

Hybrid and Kinetic Simulations of Particle Dynamics in Coaxial Plasma Jet Accelerators*

C. Thoma, T. P. Hughes, D. R. Welch, R.E. Clark
Voss Scientific, Albuquerque, NM

Collaborators:

D. Witherspoon, M. Phillips, *HyperV Technologies Corp.*

P. Hakel, *University of Nevada Reno*

J. MacFarlane, I. Golovkin, *Prism Computational Sciences*

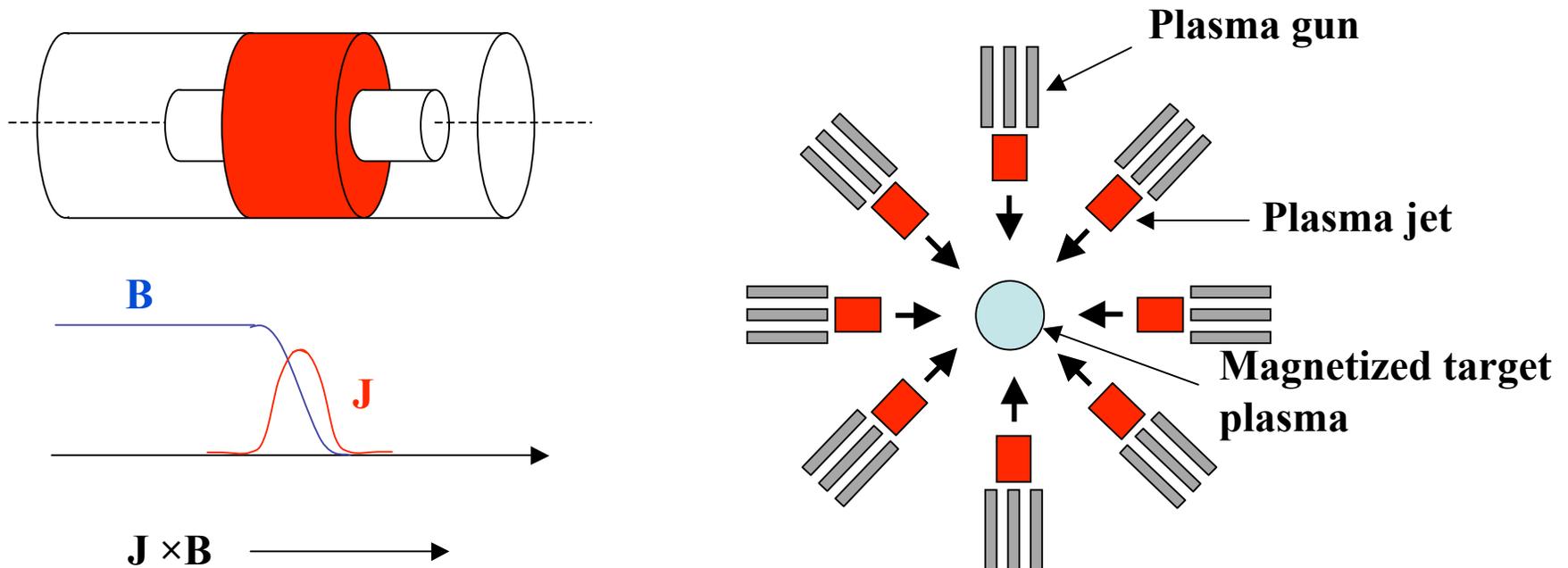
J-S Kim, S. Galkin, *FAR-TECH, Inc.*

*Work supported by DOE Office of Fusion Energy Science through HyperV Technologies Corp.

Topics

1. Motivation: Application of plasma jets to Magnetized Target Fusion
2. EMHD and Collisional PIC Algorithms for Plasma Jet Simulations
3. Multi-species acceleration in 1D
4. 2D coaxial simulations
5. Conclusions and Future Work

Coaxial plasma jets: Drivers for Magnetized Target Fusion (MTF)



Coax length ~ 1 m

Deuterium plasma “slug”
($\sim 10^{17}$ /cm⁻³) accelerated to
velocities ~ 200 km/s in a
few μ s.

MTF: Plasma jets merge to form an
imploding liner. *

*Y.C.F. Thio *et al*, Journal of Fusion Energy **20** 1 (2002)

EMHD and Kinetic PIC Algorithms in LSP

EMHD:

Drop electron inertia: **Do not have to resolve fast electron time-scales**

Ion species treated kinetically (including ion-ion collisions);

Electric field obtained from generalized Ohm's law.

EMHD algorithm uses constant σ calculated from initial values of T_e and n_e

$$\sigma = \frac{n_e e^2}{m_e \nu_{ei}} \propto T_e^{3/2}$$

Implicit Kinetic PIC:

At somewhat lower densities can run fully kinetic simulations using Direct Implicit model in LSP*.

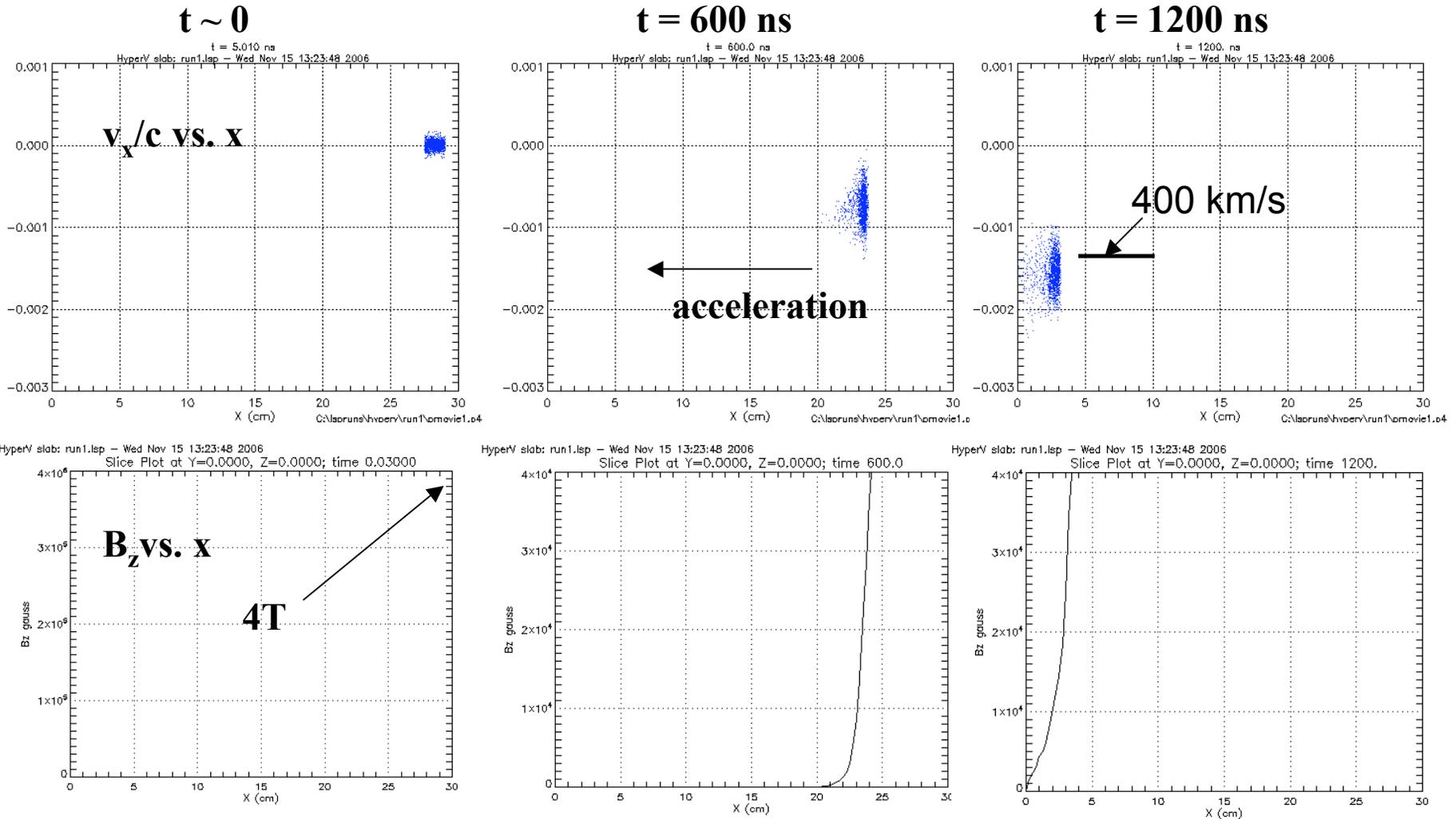
Spitzer collision model for electrons and ions

* D.R. Welch, D.V. Rose, M.E. Cuneo, R.B. Campbell, and T.A. Mehlhorn, Phys. Plasmas 11, 751 (2004)

EMHD simulation of plasma jet acceleration in $1.2\mu\text{s}$

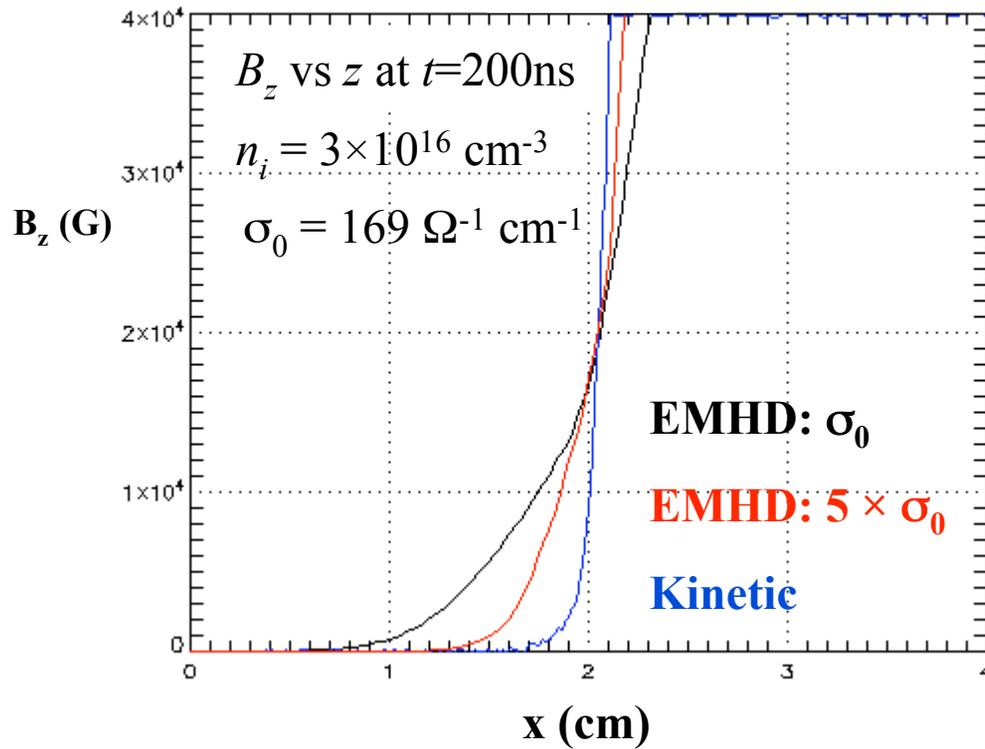
$$n_i = 3 \times 10^{17} \text{ cm}^{-3} \quad (\rho = 10^{-6} \text{ g/cm}^{-3}) \text{ Deuterium}$$

$$T_i = 5 \text{ eV} = T_e$$



**Propagates 30 cm in $1.2 \mu\text{s}$, in agreement with slug model.
Some axial heating of ions is seen**

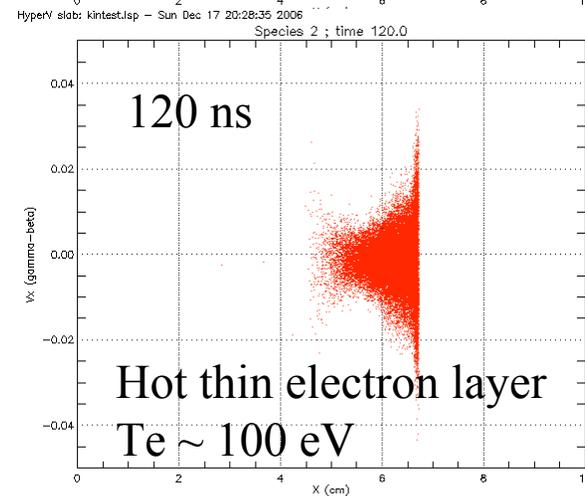
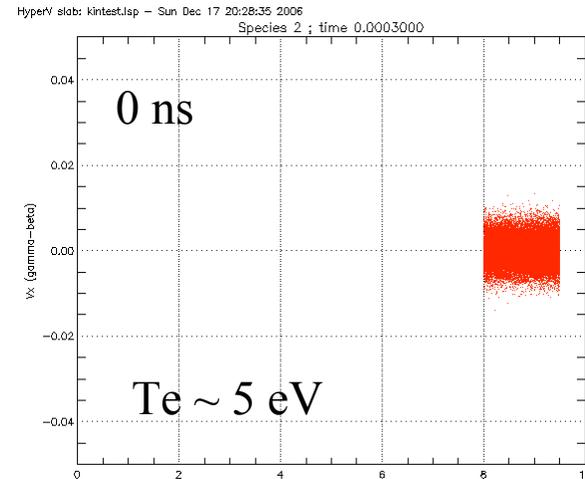
Kinetic diffusion layer thinner than EMHD layer due to large electron heating



Diffusion layer gets thinner for EMHD simulation with increased conductivity

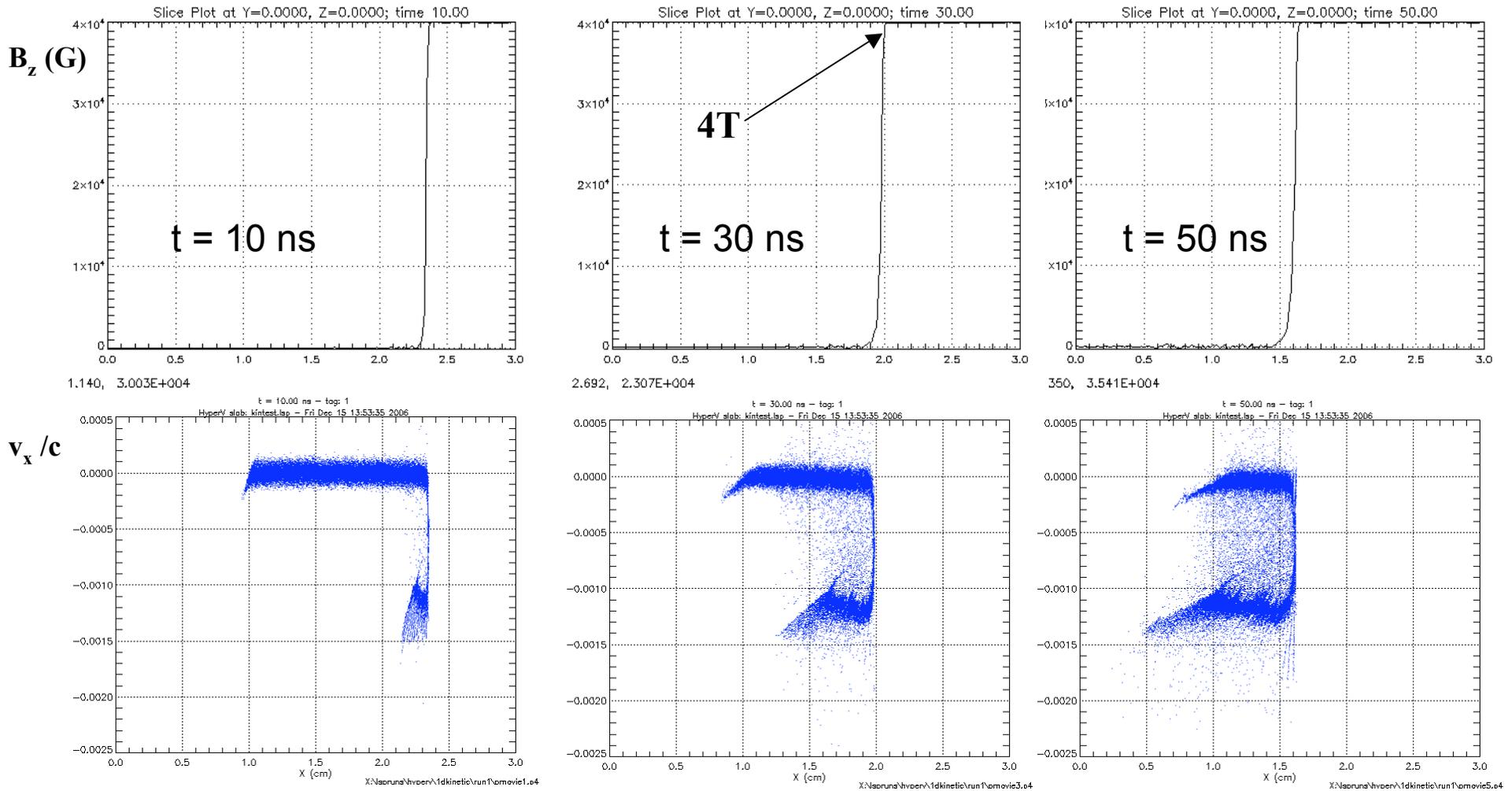
$$\sigma \propto T_e^{3/2}$$

Electron phase-space



Increased local conductivity

For large fields ions accelerated ballistically in thin diffusion layer



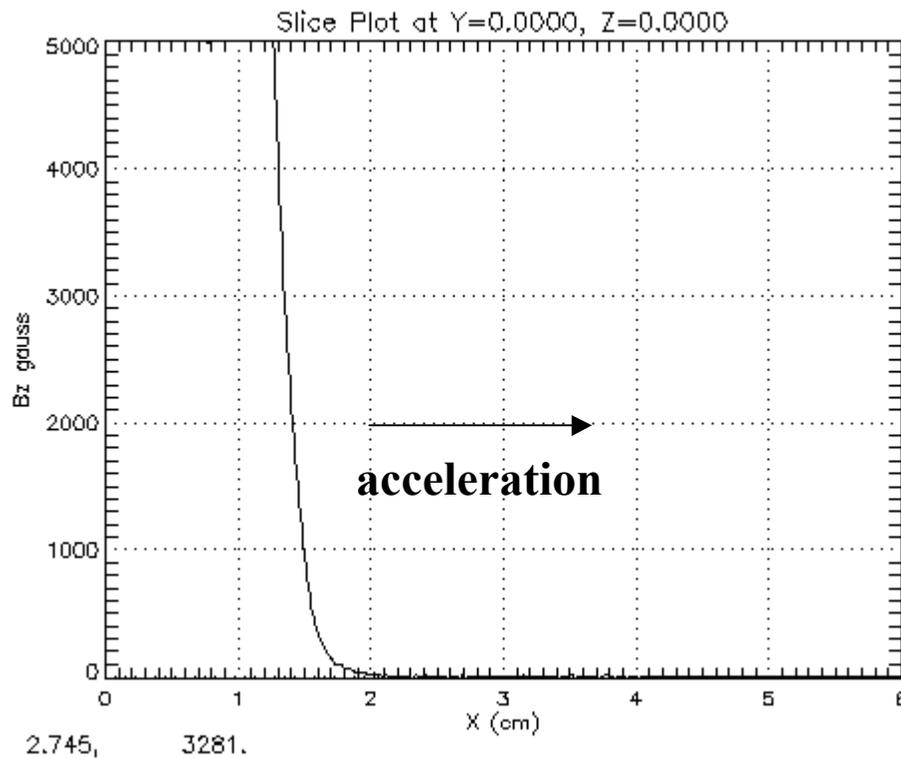
**Accelerated ions have much increased mean-free-path
Ion-ion collisions “fill-in” the phase-space**

Different ion dynamics at lower field values

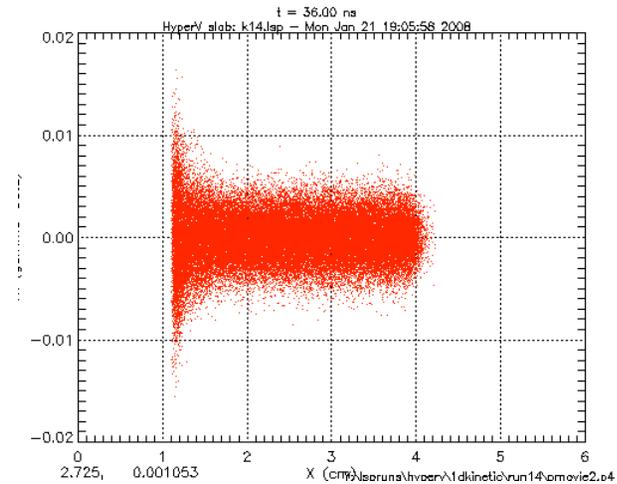
$$B_z = 0.5 \text{ Tesla}$$

$$n_i = 10^{16} \text{ cm}^{-3} \text{ Deuterium}$$

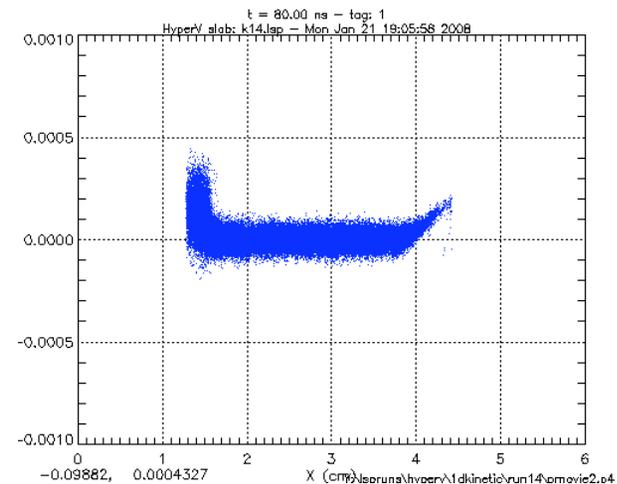
$$T_i = 5 \text{ eV} = T_e$$



Thicker diffusion layer



Less ohmic heating of electrons



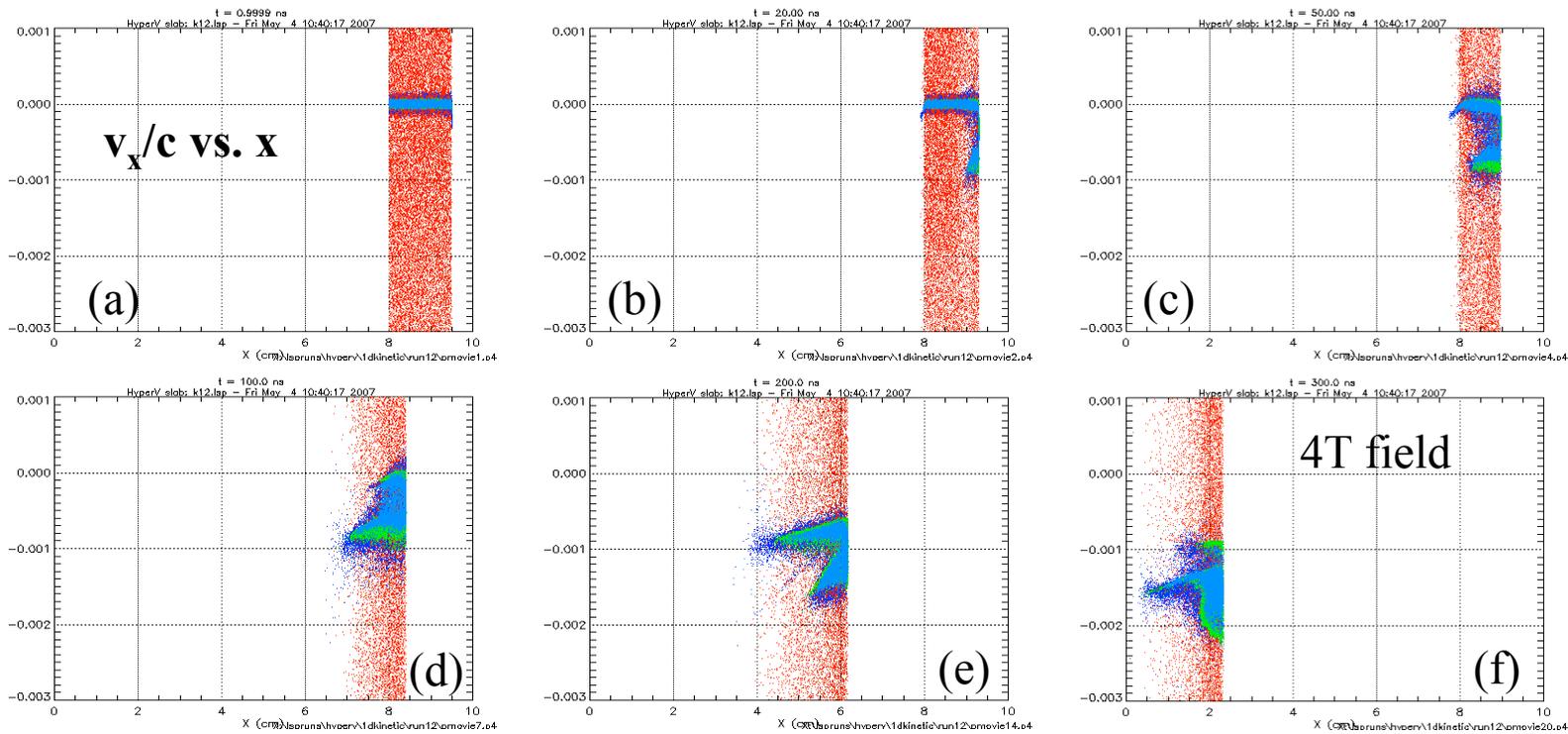
Ions collisional in sheath

Acceleration of mixed-species jet

HyperV jet is composed of 2 parts Hydrogen to 1 part Carbon

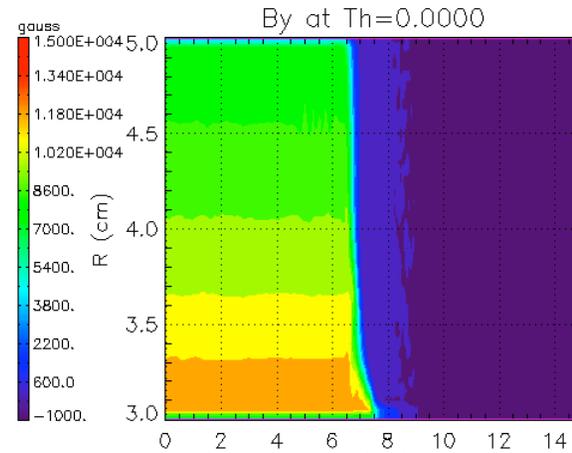
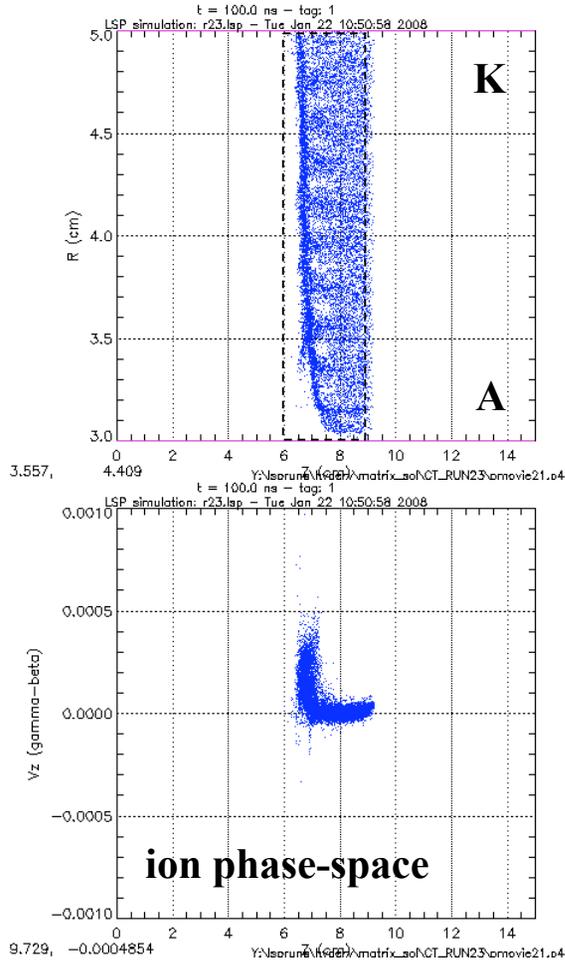
Simulations show mixture remains relatively homogeneous

$e^- : n = 3.5 \times 10^{16} \text{ cm}^{-3}$
 $D^+ : n = 2 \times 10^{16} \text{ cm}^{-3}$
 $C^+ : n = 0.5 \times 10^{16} \text{ cm}^{-3}$
 $C^{2+} : n = 0.5 \times 10^{16} \text{ cm}^{-3}$



$t =$ (a) 1 (b) 20 (c) 50 (d) 100 (e) 200 (f) 300 ns

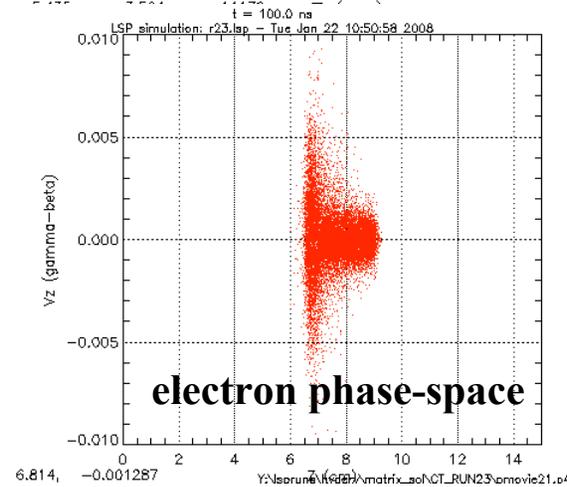
2D cylindrical coax simulations undertaken to investigate modifications to 1-D predictions



$$n_0 = 3 \times 10^{16} \text{ cm}^{-3}$$

$$T_0 = 5 \text{ eV}$$

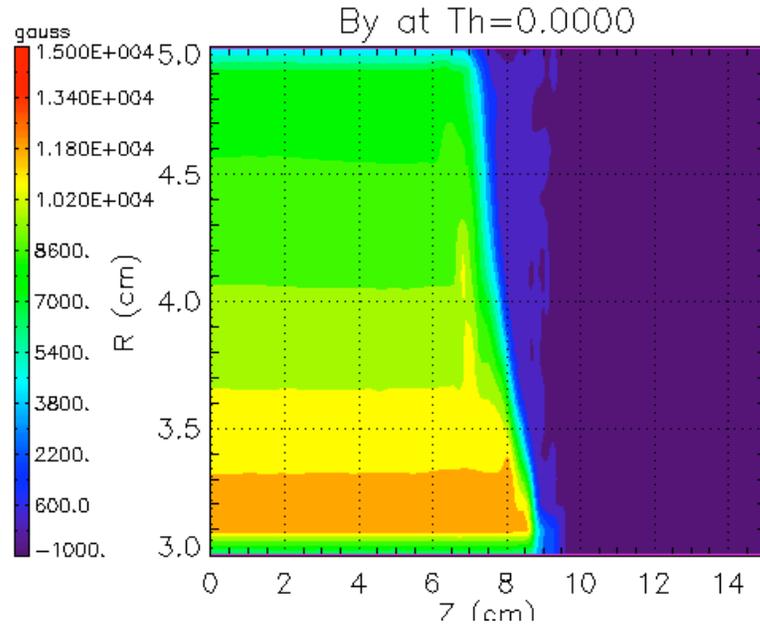
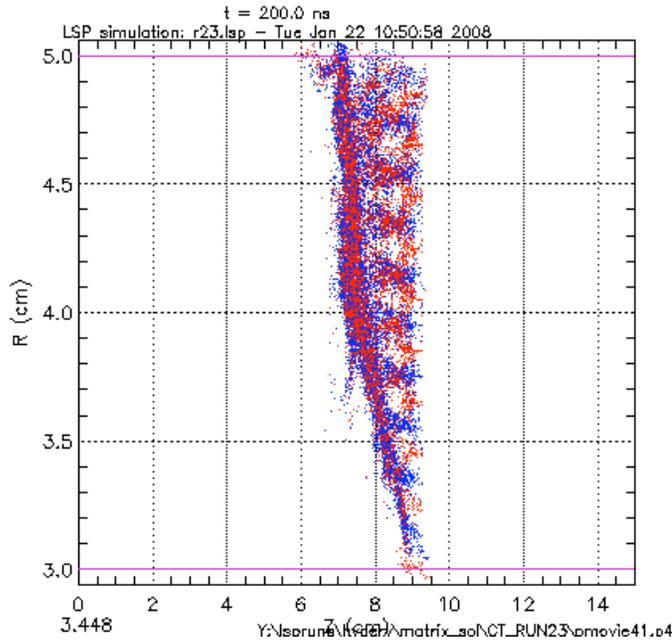
$$B_\theta \sim 1.2 \text{ T}$$



Modified version of “Direct-Implicit” algorithm in Lsp run with large time-step

$$\omega_{pe} \Delta t \sim 40$$

Plasma Erosion at Anode



$$n_0 = 3 \times 10^{16} \text{ cm}^{-3}$$

$$T_0 = 5 \text{ eV}$$

$$B_\theta \sim 1.2 \text{ T}$$

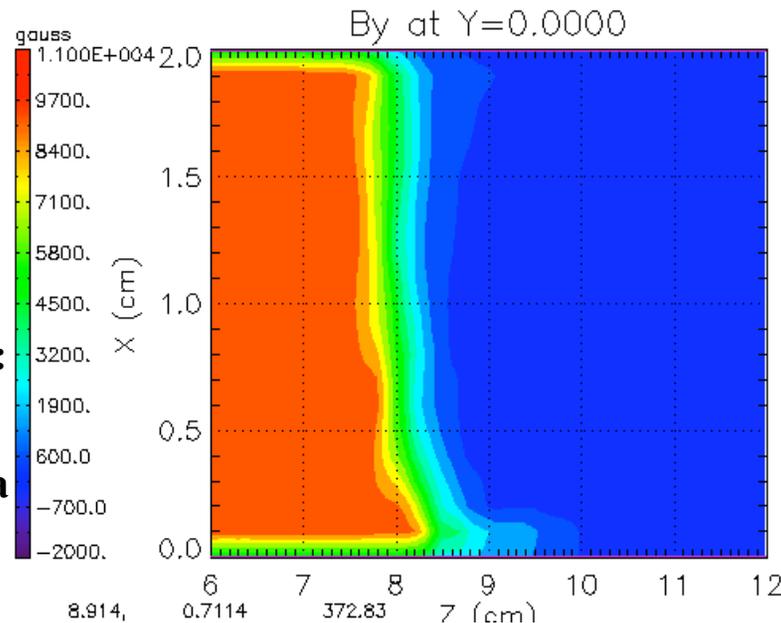
$$B_\theta \approx 1.2 \text{ T}$$

**Thinning of plasma at anode:
 “snowplow” ion acceleration plus
 “blow-by” instability?**

**But similar effect seen in planar
 geometry.**

**Note: Impractical to resolve Debye sheath:
 10^{-5} cm ($\Delta r = 1 \text{ mm}$!)**

**Large cell size may increase rate of plasma
 erosion at anode.**

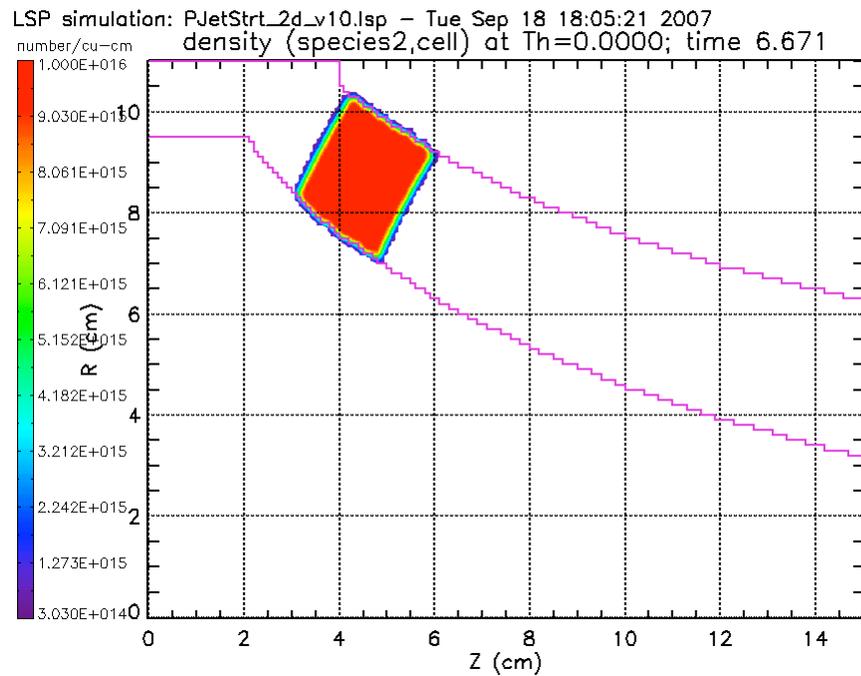


**Planar
 Geometry**

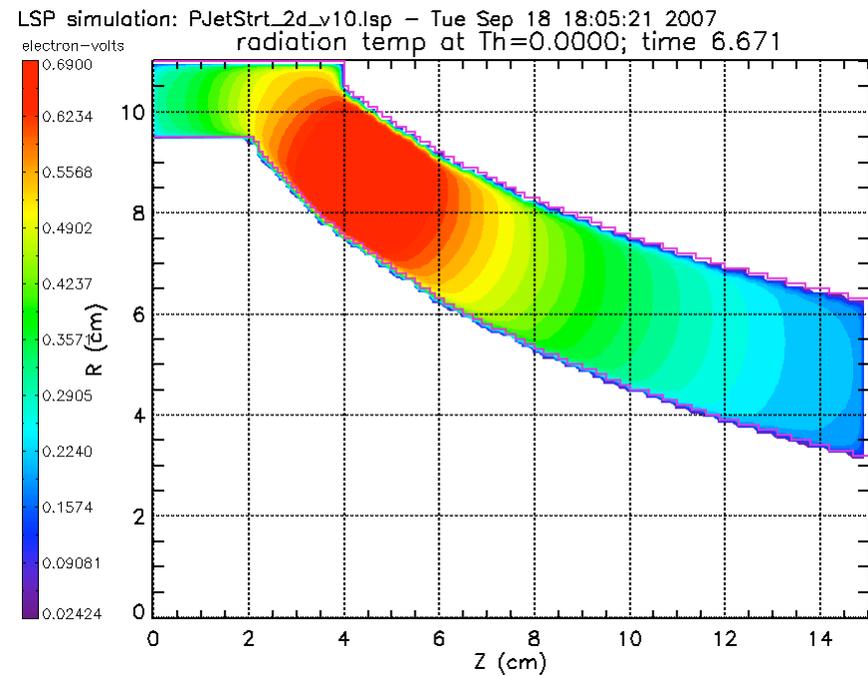
$$B_y = 1 \text{ T}$$

Work in progress with PCS to access opacity, EOS tables

CH₂ plasma, 10¹⁶ cm⁻³, 5 eV



Radiation output



Multi-group radiation diffusion model ported to LSP and parallelized

Summary of Results

Compared EMHD to kinetic-collisional PIC simulation in 1-D for plasma density of $3 \times 10^{16} \text{ cm}^{-3}$.

Obtain similar ion dynamics from both algorithms.

Kinetic simulations show strong electron heating at vacuum interface

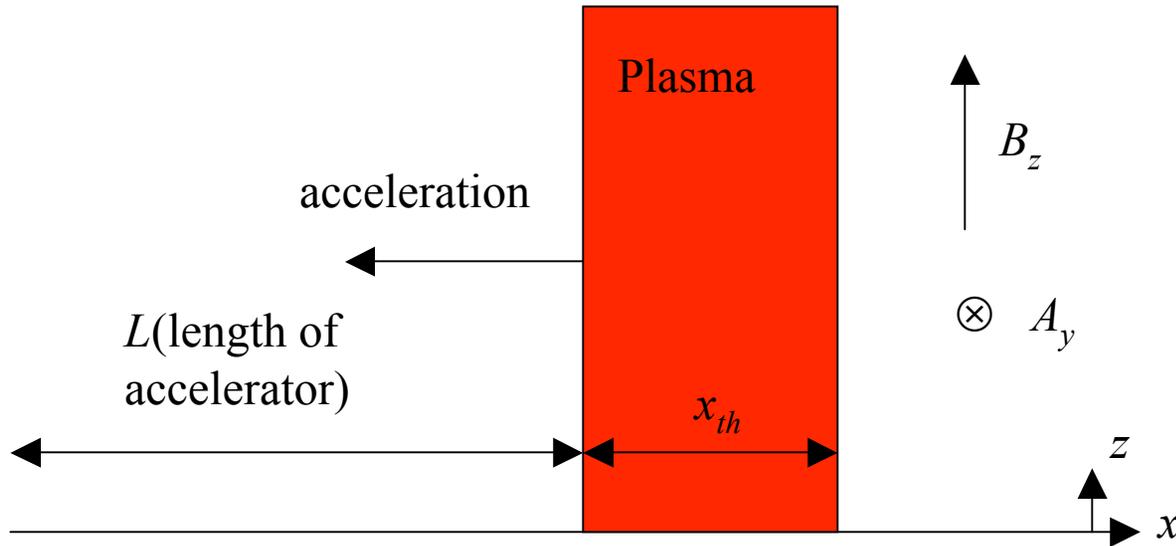
Significantly increases Hall parameter at interface

Multi-species jet simulations show mixture remains homogeneous

2D EM coaxial plasma jet simulations feasible but may require mitigation of plasma erosion at electrode surfaces.

In progress with PCS: EOS model to obtain ion charge-states from n_i, T_e

1-D plasma jet geometry



Ideal equation of motion:

$$\rho \Delta A x_{th} \frac{dv_x}{dt} = \frac{B_z^2}{2\mu_o} \Delta A$$

Slug acceleration:

$$a = \frac{B_z^2}{2\mu_o \rho x_{th}}$$

Final velocity:

$$v_f = \sqrt{2aL}$$

The time to reach the end
of the accelerator:

$$t_f = 2L / v_f$$

Different q/m ions accelerated to same velocity

Estimate of impulse for plasma with (total)
mass density ρ

$$\Delta v/c \approx 9.4 \times 10^{-12} [\Delta B/G] \left[\frac{\rho}{\text{g/cm}^3} \right]^{-1/2}$$

$$\Delta B \sim 4 \times 10^4 \text{ G}$$

$$\rho \sim [2 \cdot 2 \times 10^{16} + 12 \cdot 2 \cdot 0.5 \times 10^{16}] m_p \cdot \text{cm}^{-3} = 2.7 \times 10^{-7} \text{ g/cm}^3$$

$$\Delta v/c \sim 0.00073$$

More massive ions penetrate deeper into the diffusion layer, and experience a larger total force which compensates for their greater inertia.

